

Systems of Equations Practice

1. Terry has a collection of fifty basketball cards. The National Basketball Association cards are worth \$3.50 and the collegiate basketball cards are worth \$2.00 each. Terry's collection is worth \$122.50.

Write and solve a system of linear equations that can be used to determine the number of each type of card Terry has. State the solution in the context of the problem.

15 X = NBA
35 y = college

$$\begin{aligned} x + y &= 50 & x &= 50 - y \\ 3.50x + 2.00y &= 122.50 \\ 3.50(50 - y) + 2y &= 122.50 \\ 175 - 3.50y + 2y &= 122.50 \end{aligned}$$

$$\begin{aligned} -1.50y &= -52.50 \\ y &= 35 \\ x + y &= 50 & x &= 15 \\ x + 35 &= 50 \end{aligned}$$

2. At the grocery store, artichokes are one price and avocados are another. Thomas buys three artichokes and one avocado for \$2.70. Cara buys one artichoke and 4 avocados for \$6.40.

Write and solve a system of equations that can be used to determine the cost of artichokes and avocados. State the solution in the context of the problem.

\$1.40
X artichokes
\$1.50
y avocados

$$\begin{aligned} 3x + y &= 2.70 \\ -3(1x + 4y &= 6.40) \\ \hline 3x + y &= 2.70 \\ -3x - 12y &= -19.20 \\ \hline -11y &= -16.50 \\ y &= 1.5 \end{aligned}$$

$$\begin{aligned} 3x + 1.5 &= 2.70 \\ 3x &= 1.20 \\ x &= .4 \end{aligned}$$

Solve each system using any method.

3. $3x + 4y = 10$
 $4x - 4y = 11$

$$\begin{aligned} 7x &= 21 \\ x &= 3 \\ (3, \frac{1}{4}) \end{aligned}$$

$$\begin{aligned} 3x + 4y &= 10 \\ 3(3) + 4y &= 10 \\ 9 + 4y &= 10 \\ 4y &= 1 \\ y &= \frac{1}{4} \end{aligned}$$

4. $2x + 5y = 15$ $-6x + 15y = 45$
 $6x - 3y = 9$ $6x - 3y = 9$

$$\begin{aligned} 12y &= 54 \\ y &= 4.5 \\ 6x - 3(4.5) &= 9 \\ 6x - 13.5 &= 9 \\ 6x &= 22.5 \\ x &= 3.75 \end{aligned}$$

5. $y = 3x + 7$
 $4x + 2y = 12$

$$\begin{aligned} 4x + 2(3x + 7) &= 12 \\ 4x + 6x + 14 &= 12 \\ 10x &= -2 \\ x &= -\frac{2}{10} = -\frac{1}{5} \\ y &= 3(-\frac{1}{5}) + 7 \\ &= -\frac{3}{5} + 7 \\ &= -\frac{3}{5} + \frac{35}{5} = \frac{32}{5} \end{aligned}$$

6. $6x - 4y = 17$
 $3x + 4y = 10$

$$\begin{aligned} 9x &= 27 \\ x &= 3 \\ (3, \frac{1}{4}) \end{aligned}$$

$$\begin{aligned} 3(3) + 4y &= 10 \\ 9 + 4y &= 10 \\ 4y &= 1 \\ y &= \frac{1}{4} \end{aligned}$$

7. $4x = 10y + 2$
 $2y = x - 14$

$$\begin{aligned} 2y + 14 &= x \\ 4(2y + 14) &= 10y + 2 \\ 8y + 56 &= 10y + 2 \\ 54 &= 2y \\ 27 &= y \\ (68, 27) \end{aligned}$$

8. A clothing store sells shirts for one price and sweatshirts for another price. Melanie purchases two shirts and six sweatshirts for \$60. Chad purchases four shirts and three sweatshirts for \$75.

Write and solve a system of linear equations that could be used to determine the cost of one shirt and one sweatshirt. State the solution in the context of the problem.

Shirts = x \$15
Sweatshirts = y \$5

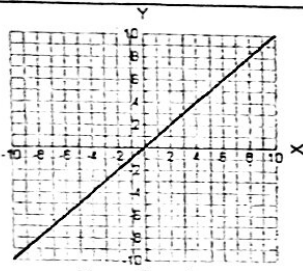
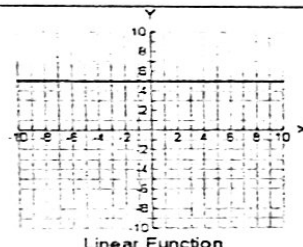
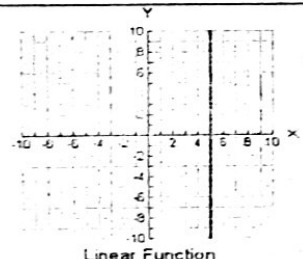
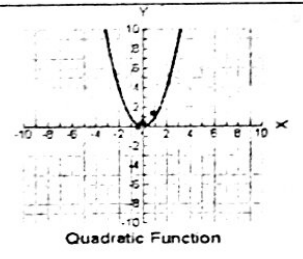
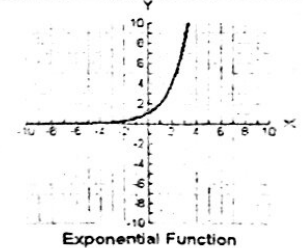
$$\begin{aligned} 2x + 6y &= 60 \\ -2(4x + 3y &= 75) \\ \hline 2x + 6y &= 60 \\ -8x - 6y &= -150 \\ \hline -6x &= -90 \\ x &= 15 \end{aligned}$$

$$\begin{aligned} 2(15) + 6y &= 60 \\ 30 + 6y &= 60 \\ 6y &= 30 \\ y &= 5 \end{aligned}$$

Function Chart

Function – for every input there is exactly one output.

- Domain (x's) can not repeat; must pass the vertical line test

Graph Looks Like	Equation	Function Name	Function – Yes or No?	Domain? Range?												
 <p style="text-align: center;">Linear Function</p>	$y = x^1$ $y = 1x^1 + 0$ (m=1; b=0)	Linear	Yes	$D = \mathbb{R}$ $R = \mathbb{R}$												
 <p style="text-align: center;">Linear Function</p>	$y = 5$ (y = any number) $y = 0x^1 + 5$	Constant	Yes	$D = \mathbb{R}$ $R = 5$												
 <p style="text-align: center;">Linear Function</p>	$x = 5$ (x = any number)	Constant	No	$D = 5$ $R = \mathbb{R}$												
 <p style="text-align: center;">Quadratic Function</p>	$y = x^2$ <table style="margin-left: auto; margin-right: auto; border-collapse: collapse;"> <tr> <td style="border-right: 1px solid black; padding: 0 5px;">x</td> <td style="padding: 0 5px;">y</td> </tr> <tr> <td style="border-right: 1px solid black; padding: 0 5px;">0</td> <td style="padding: 0 5px;">0</td> </tr> <tr> <td style="border-right: 1px solid black; padding: 0 5px;">1</td> <td style="padding: 0 5px;">1</td> </tr> <tr> <td style="border-right: 1px solid black; padding: 0 5px;">2</td> <td style="padding: 0 5px;">4</td> </tr> <tr> <td style="border-right: 1px solid black; padding: 0 5px;">3</td> <td style="padding: 0 5px;">9</td> </tr> <tr> <td style="border-right: 1px solid black; padding: 0 5px;">4</td> <td style="padding: 0 5px;">16</td> </tr> </table>	x	y	0	0	1	1	2	4	3	9	4	16	Quadratic $Ax^2 + Bx + C$	Yes	$D = \mathbb{R}$ $R = y \geq 0$ or $[0, \infty)$
x	y															
0	0															
1	1															
2	4															
3	9															
4	16															
 <p style="text-align: center;">Exponential Function</p>	$y = 2^x$	Exponential $y = ab^x$	Yes	$D = \mathbb{R}$ $R = y > 0$ $(0, \infty)$												

\mathbb{R}

Touches
(approaches)